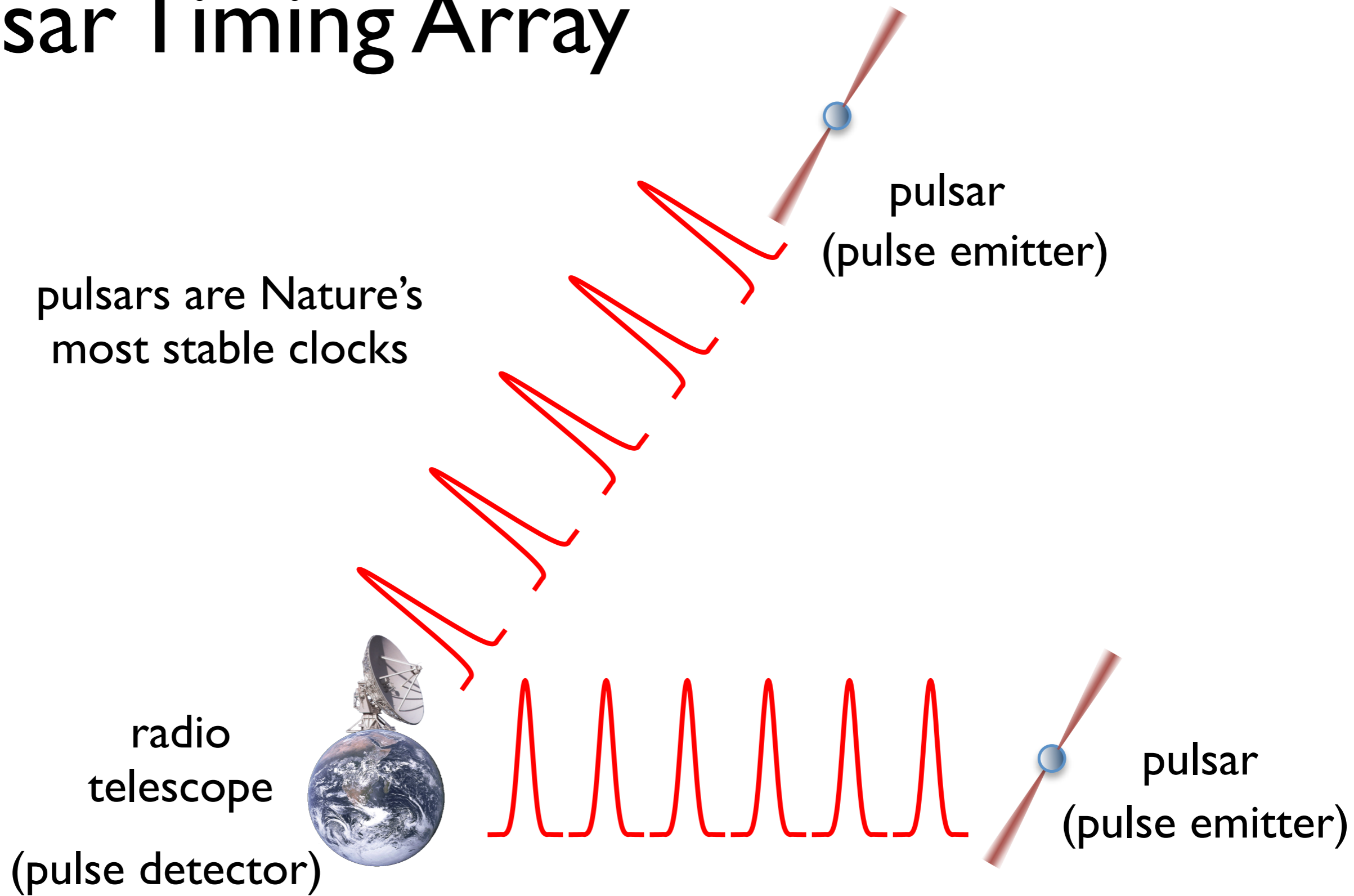


Using metronomes & microphones to model a pulsar timing array

Pulsar Timing Array

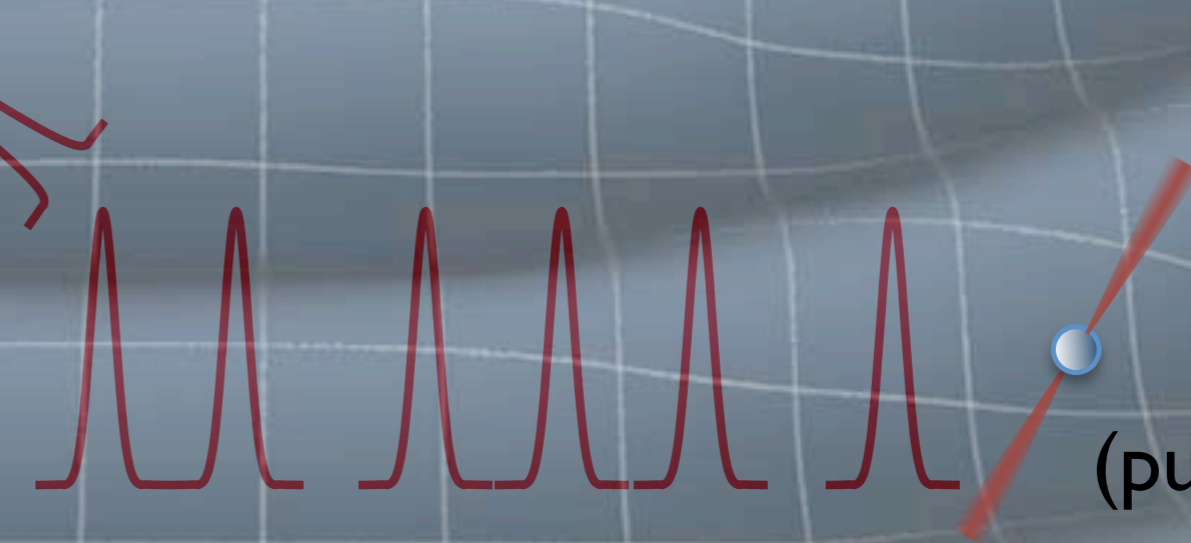


Pulsar Timing Array

gravitational waves
cause pulses to arrive
ahead or behind schedule,
correlated across pulsars
(pulse perturber)

pulsar
(pulse emitter)

radio
telescope
(pulse detector)



Metronome Timing Array

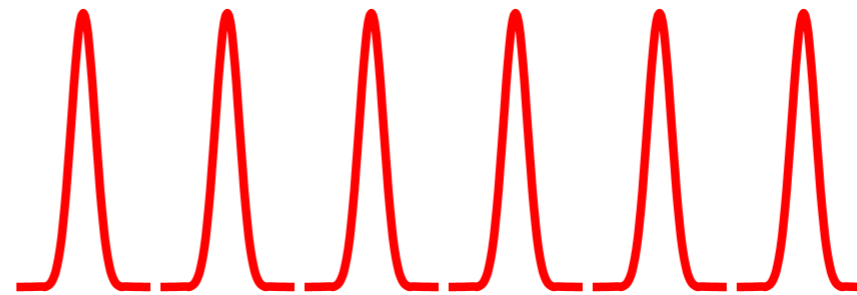
microphone motion
causes pulses to arrive
ahead or behind schedule,
correlated across metronomes
(pulse perturber)



metronome
(pulse emitter)



microphone
(pulse detector)



metronome
(pulse emitter)

Key quantities to calculate

pulse period T_p

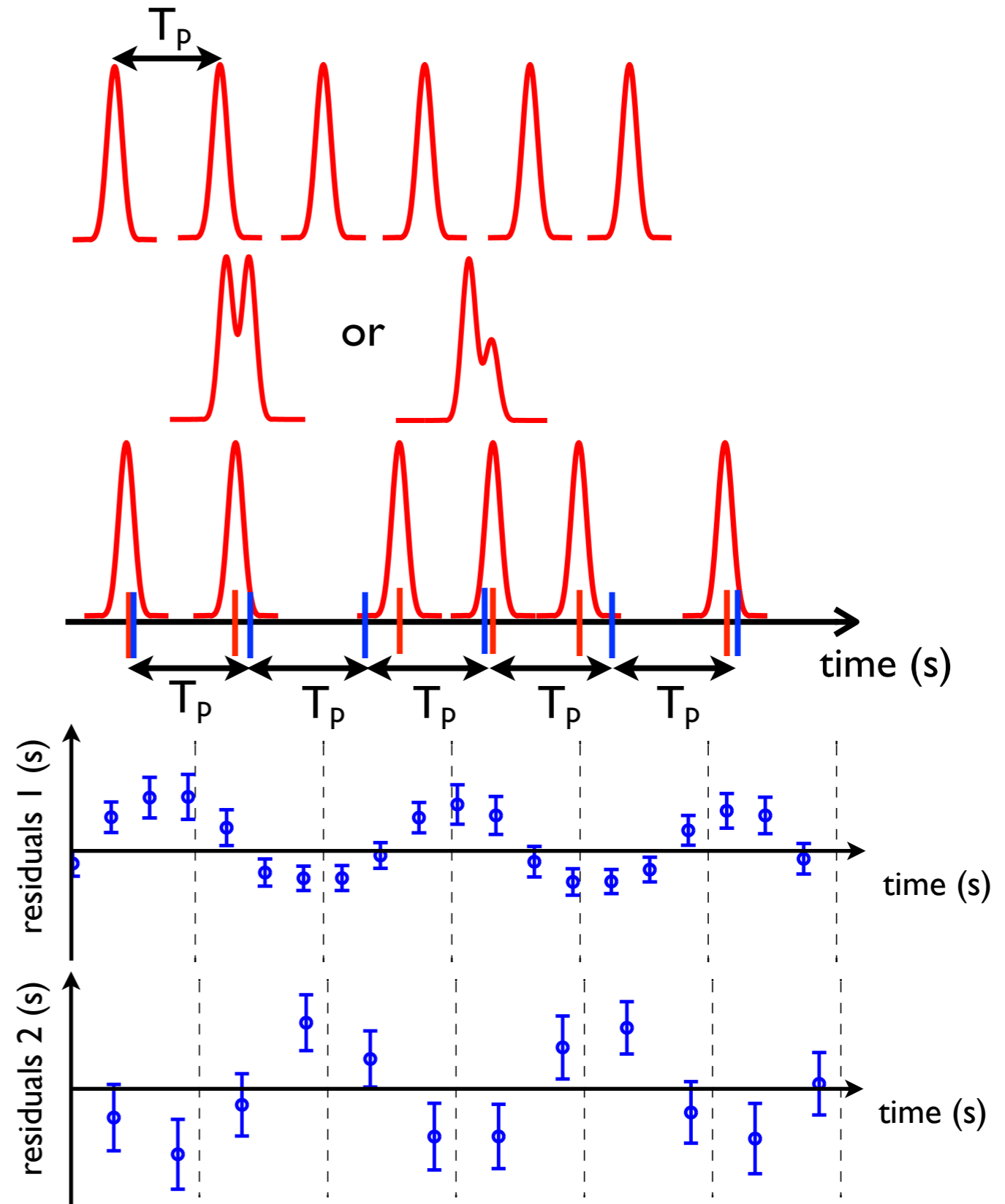
pulse shape (profile)

measured times of arrival (TOAs)

expected TOAs

residuals = measured - expected

correlations between
pairs of residuals



Some numbers to keep in mind

$$v_{\text{sound}} = 340 \text{ m/s (in air)}$$

$$\text{amplitude} \approx 10 \text{ cm}$$

$$\text{amplitude} / v_{\text{sound}} = 3 \times 10^{-4} \text{ sec}$$

$$120 \text{ bpm: } T_p = 0.5 \text{ sec}$$

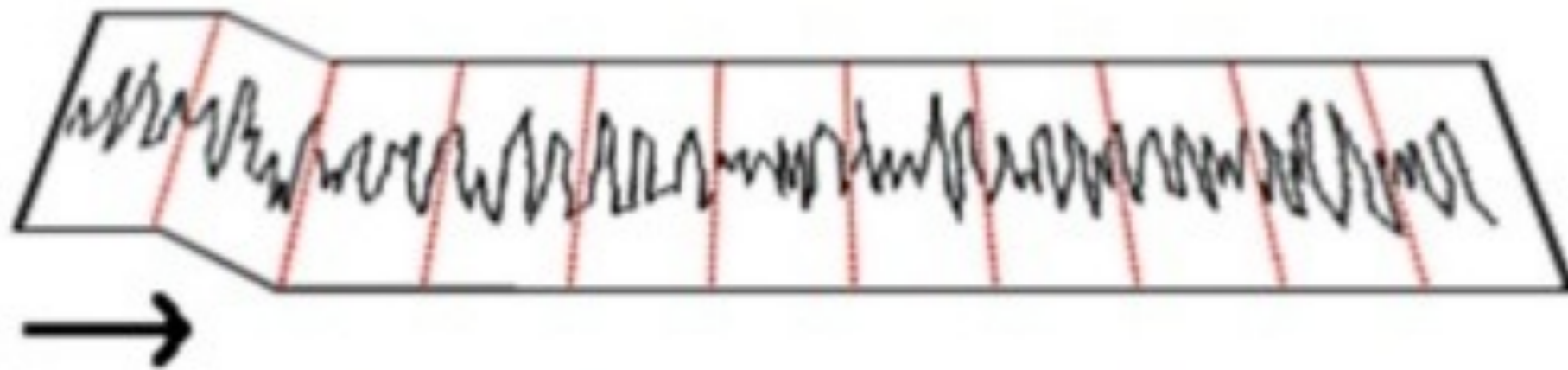
$$200 \text{ bpm: } T_p = 0.3 \text{ sec}$$

PTAdemo0GUI.py

m200a.txt

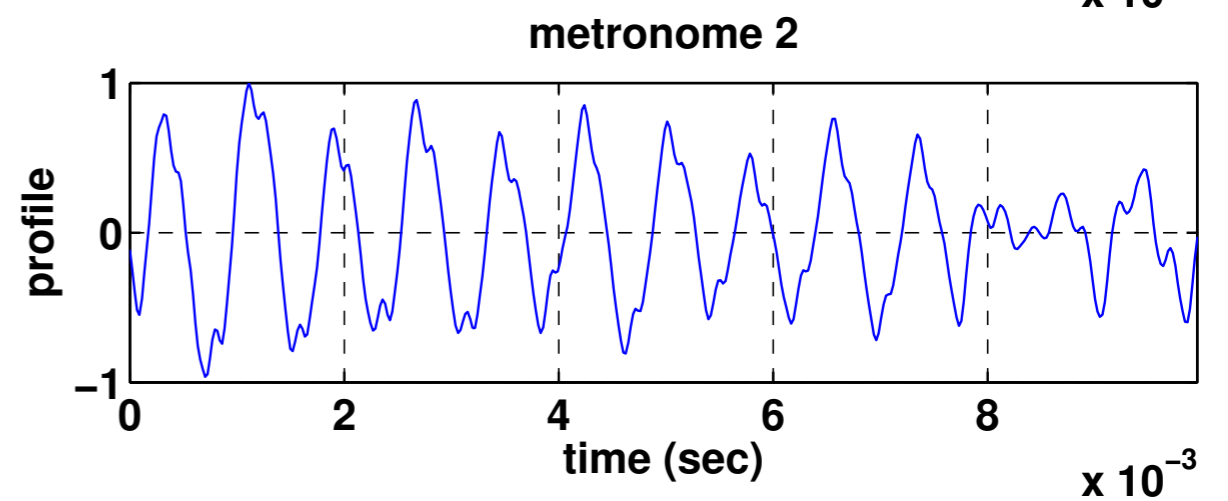
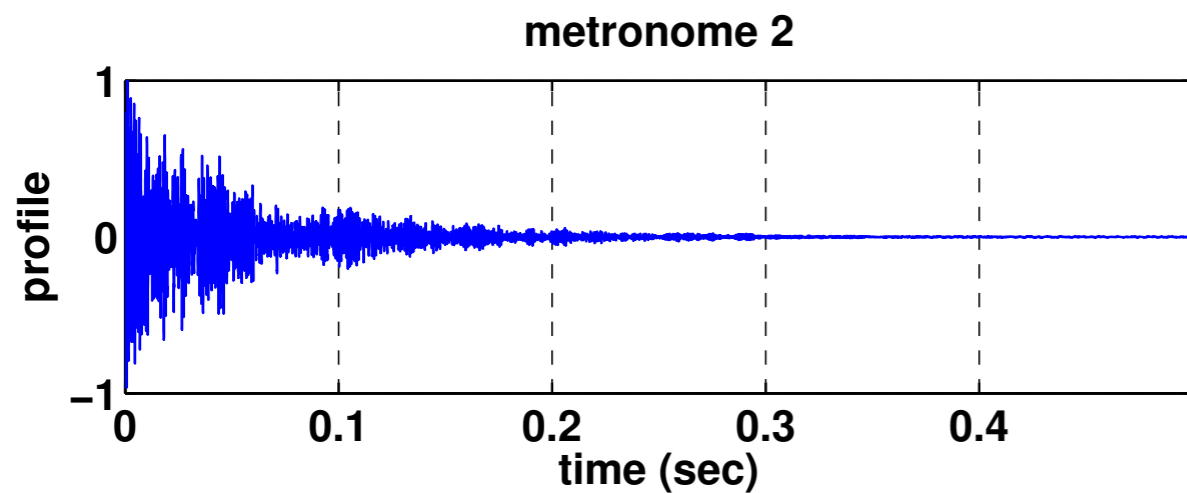
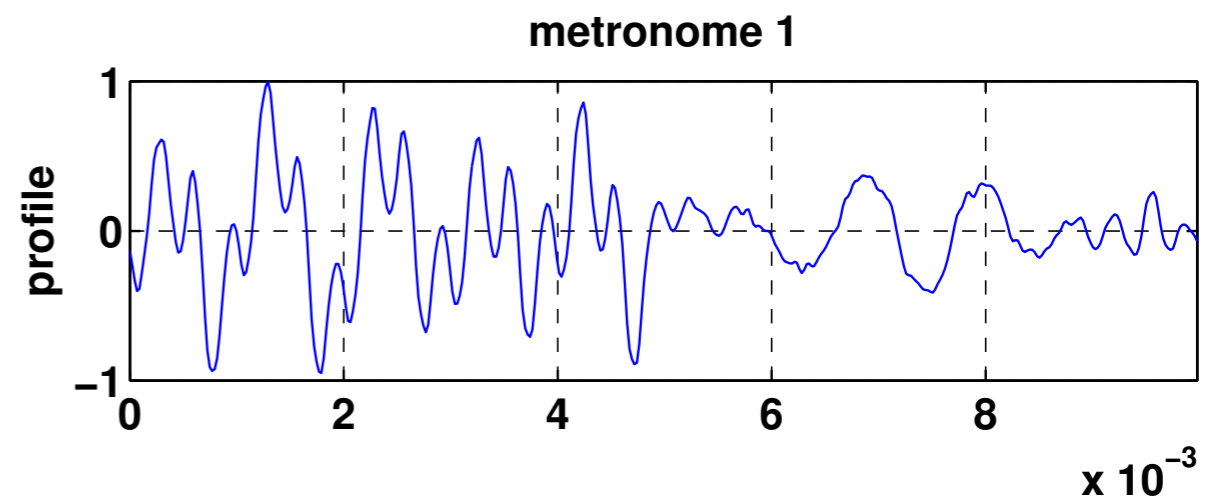
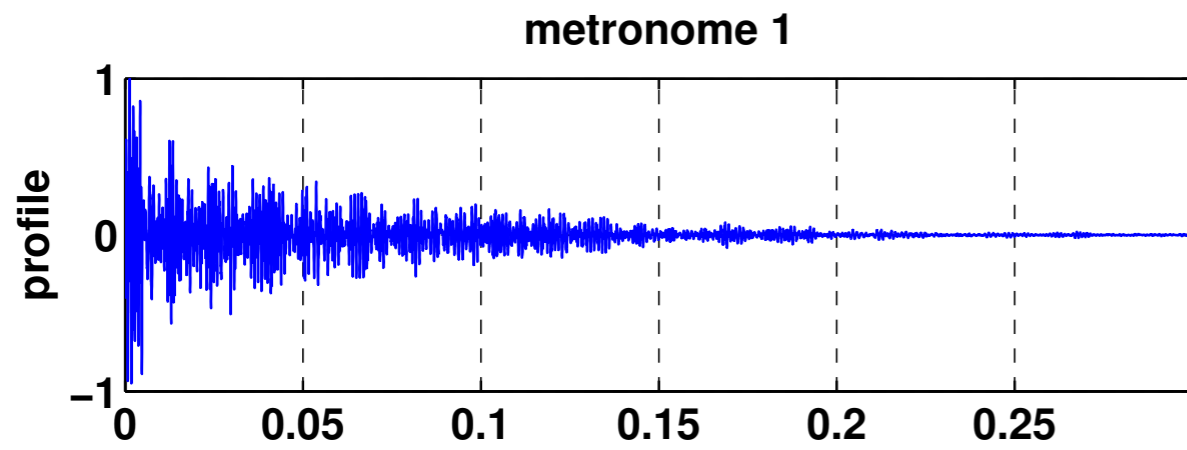
m120b.txt

Data folding to determine pulse period and pulse profile

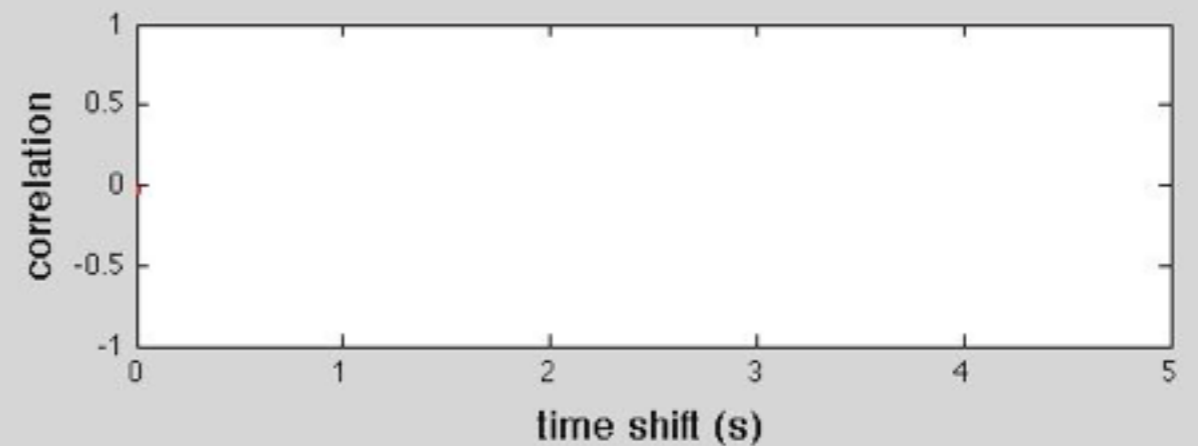
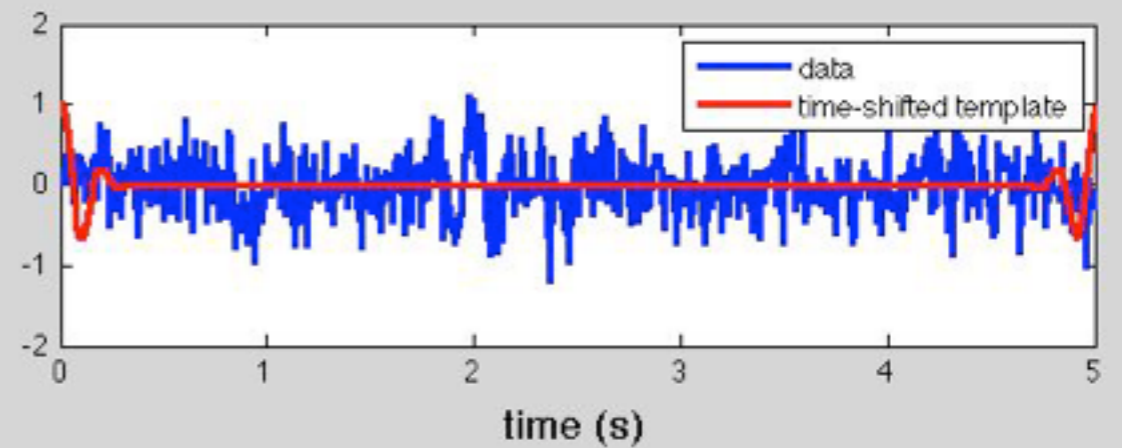
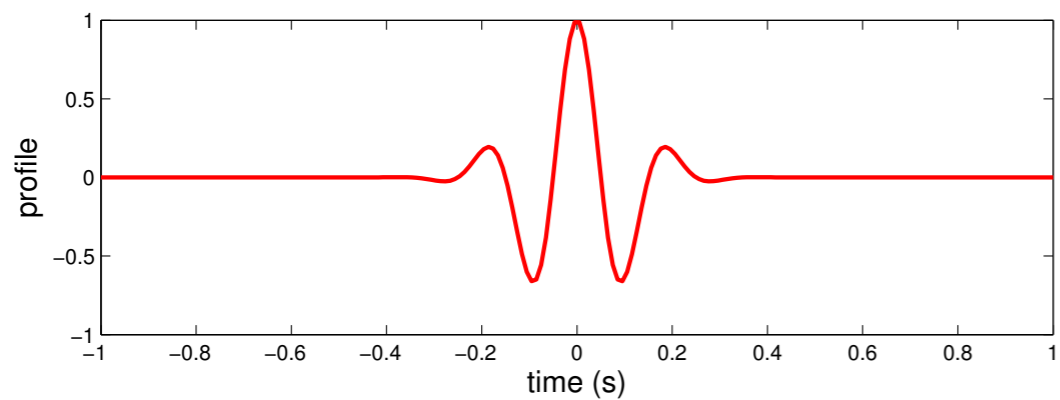
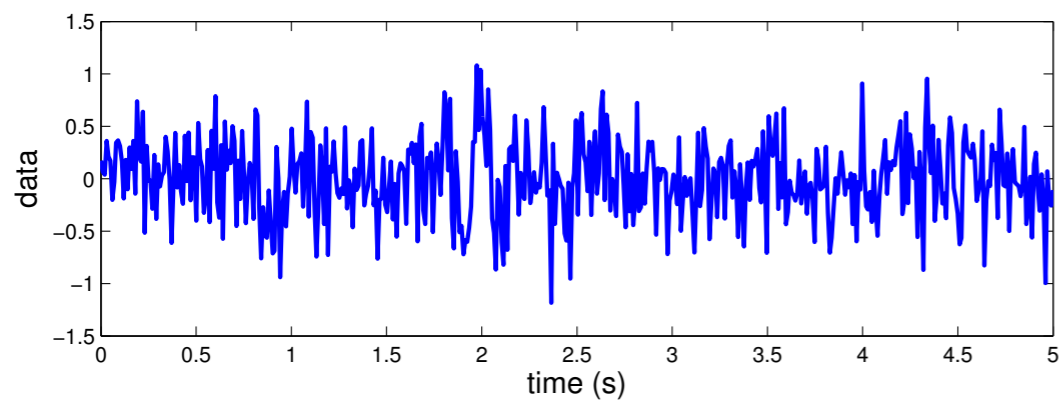


- break data into chunks of duration T
- fold (stack) chunks, then add together
- get maximum sum when T is the period of the signal (noise cancels, signal combines coherently)

Metronome pulse profiles



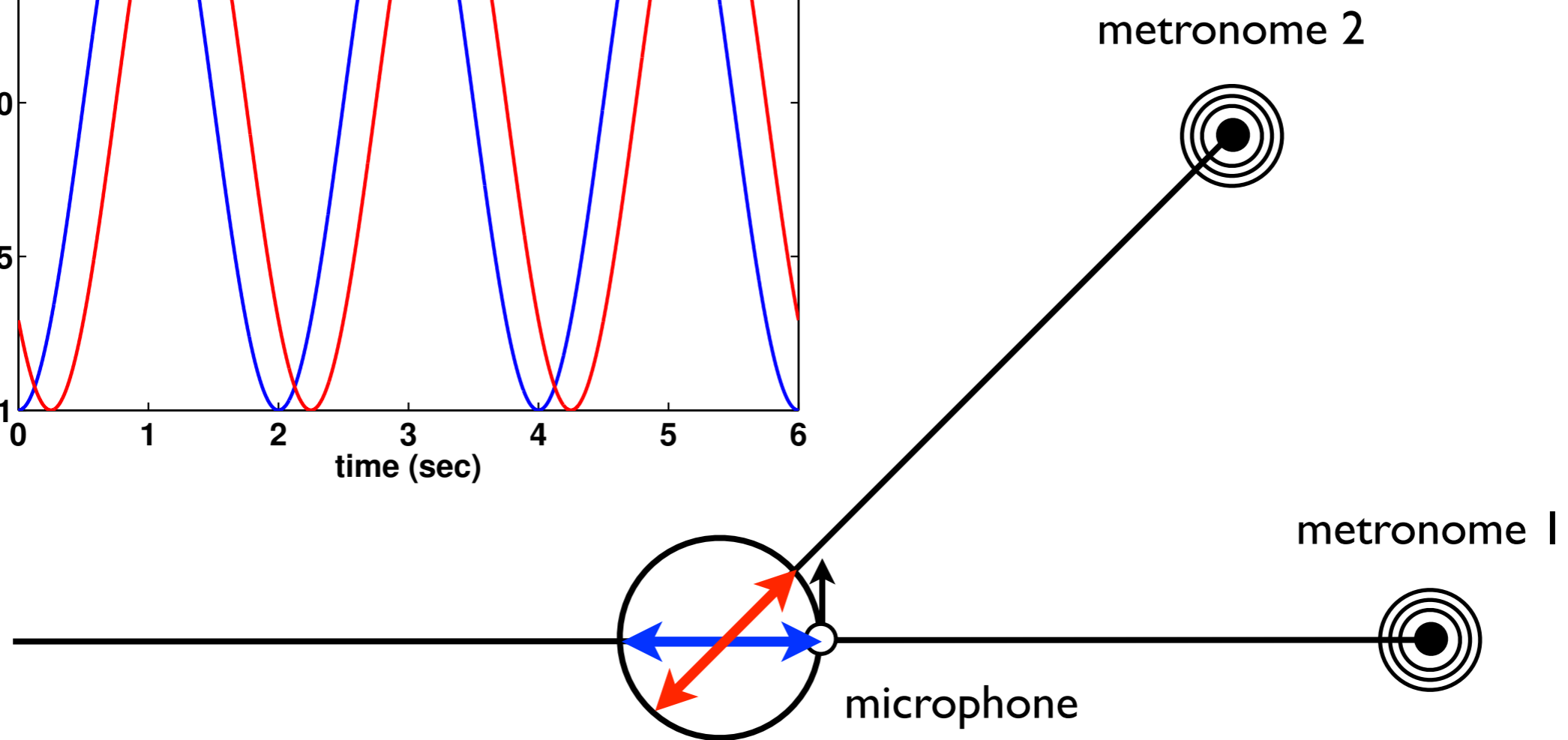
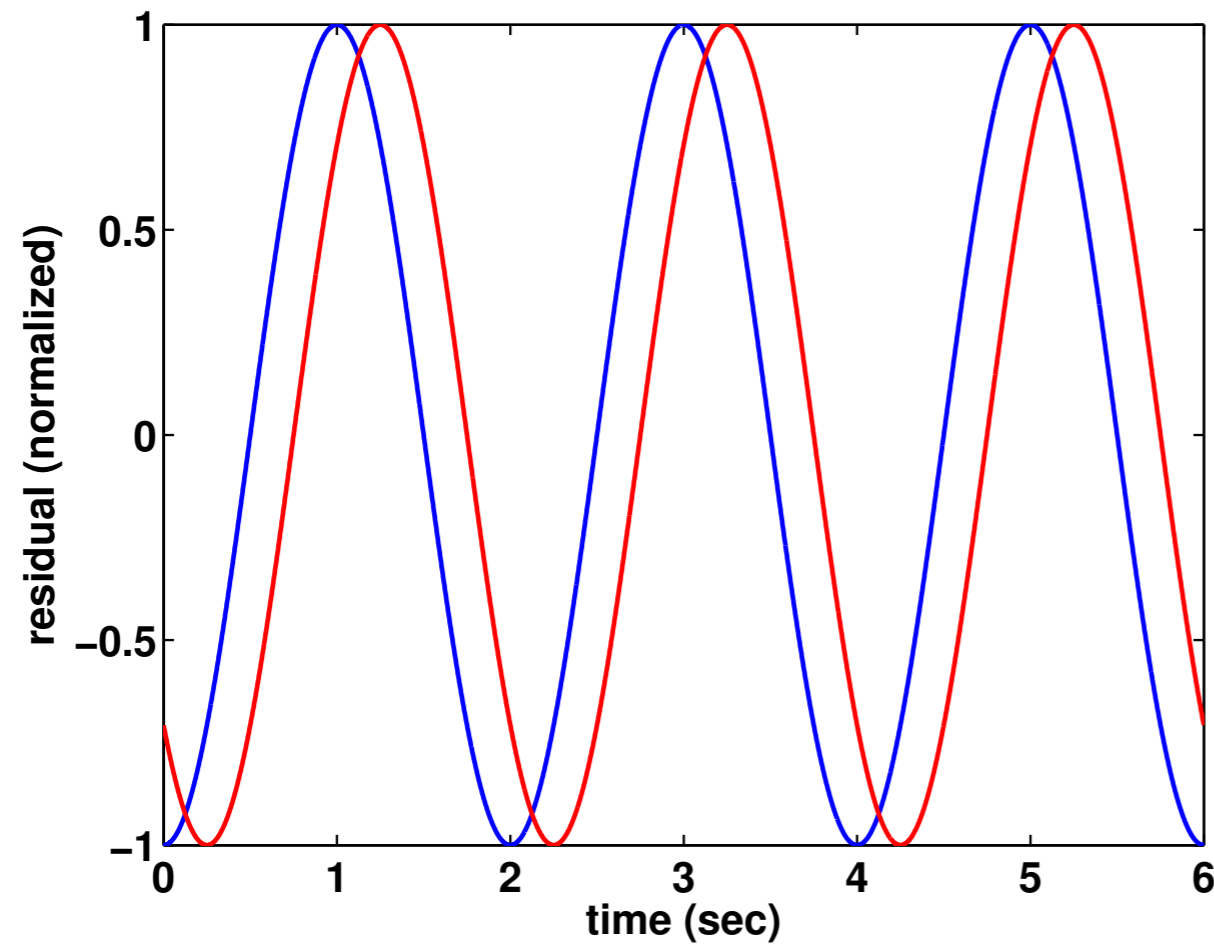
Estimating TOAs by correlating data with the pulse profile



PTAdemo2GUI.py

m200a | 20b0.txt

Expected residuals for circular microphone motion



PTAdemo2GUI.py

m200a|20b|80.txt

m200a|20b90.txt

m200a|20b45.txt

m200a|20b|35.txt

Metronome timing array illustrates several techniques from pulsar timing

1. Estimate pulse period and pulse shape (profile) by folding data
2. Estimate pulse times of arrival (TOAs) by correlating data with pulse profile
3. Calculate timing residuals by subtracting expected TOAs (based on a model) from the measured TOAs
4. Improve estimate of pulse period by removing a linear trend from residuals
5. Timing residuals for a pair of pulsars are correlated as a function of their angular separation